



Beam lifetime

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The ninth KEKB Accelerator Review Committee

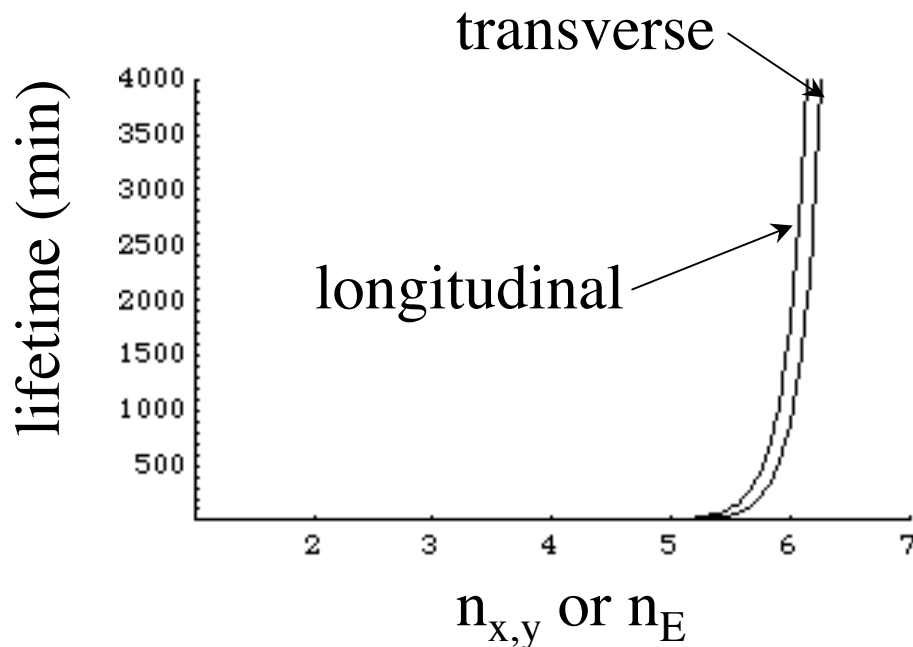
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KEK

Quantum lifetimes

- Particle losses occurs for Gaussian beam due to finite transverse or energy aperture.
- Quantum lifetime is not serious problem in principle.
- Transverse : mask aperture / longitudinal : momentum aperture.

$$\tau_q = \frac{\tau_u}{2} \frac{e^{\xi_u}}{\xi_u} \quad u = x, y, s$$



$$\xi_{x,y} = \frac{1}{2} \left(\frac{A_{x,y}}{\sigma_{x,y}} \right)^2 = \frac{1}{2} n_{x,y}^2$$

$$\xi_s = \frac{1}{2} \left(\frac{\Delta E / E_0}{\sigma_E / E_0} \right)^2 = \frac{1}{2} n_E^2$$

Vacuum lifetime

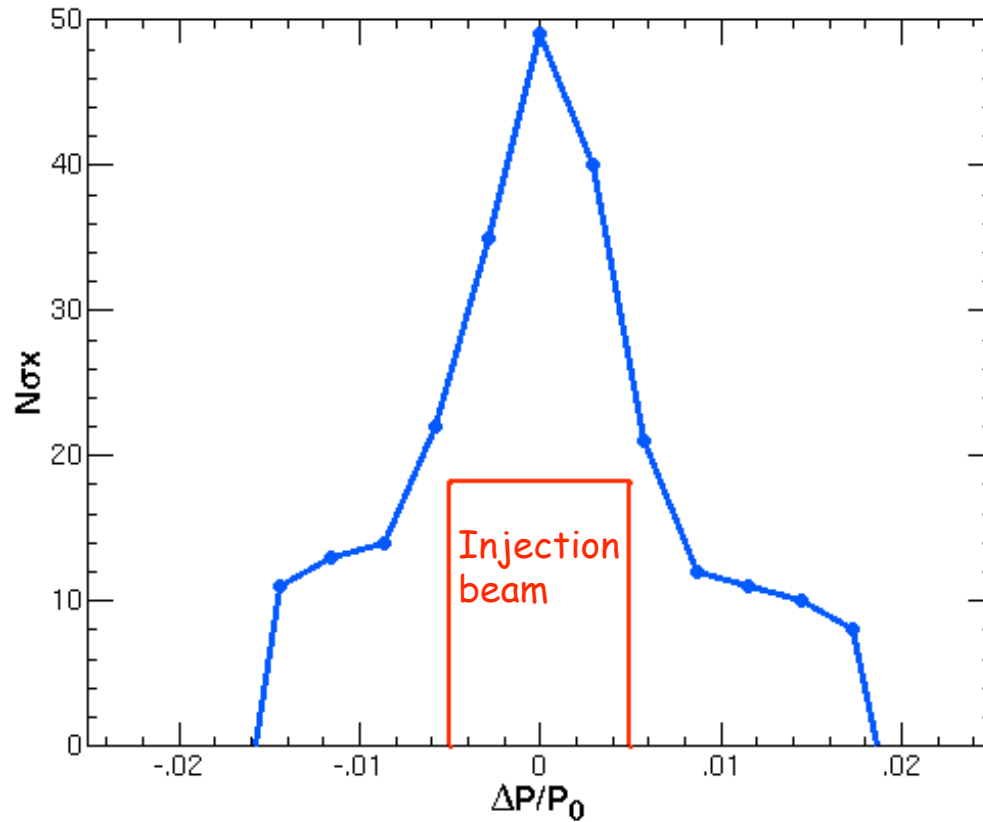
- Bremsstrahlung
- Pressure $\sim 5 \times 10^{-7}$ Pa.
- Vacuum lifetime is expected to be ~ 10 hours for LER and HER.

Touschek lifetime

Momentum aperture determines lifetime.

LER lifetime is shorter than HER.

$$\text{LER } \beta_x^*/\beta_y^* = 20/0.3\text{cm } J_y/J_x = .16$$



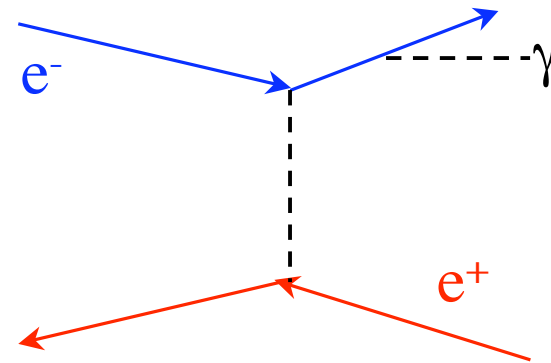
- Dynamic aperture in LER
- Machine errors are not included.
- Transverse aperture is acceptable.

SuperKEKB-LER

Coupling	Lifetime
1%	51 min
2%	72 min
4%	102 min
6%	145 min

Luminosity lifetime

Luminosity lifetime is determined by cross section of radiative Bhabha and luminosity.



Particle loss rate :

$$\frac{dN}{dt} = -\sigma L$$

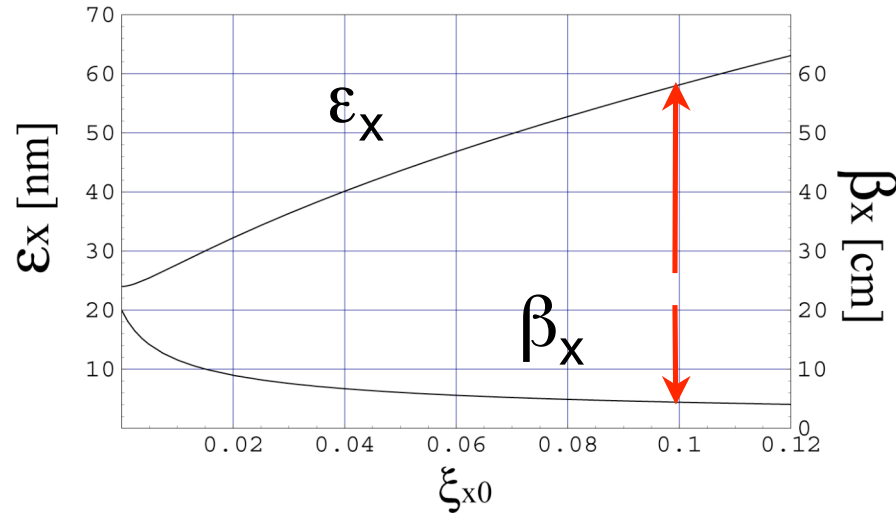
$$\sigma = \frac{16\alpha r_e^2}{3} \left[\left(\log \frac{1}{\varepsilon} - \frac{5}{8} \right) \left\{ \log \left(\frac{2\sqrt{2}\pi\sigma_y^*}{\lambda_e} \right) + \frac{\gamma_E}{2} \right\} + \frac{1}{4} \left(\frac{13}{3} \log \frac{1}{\varepsilon} - \frac{17}{6} \right) \right]$$

$$\varepsilon = \Delta E / E_0$$

$$\sigma = 2 \times 10^{-25} \text{ cm}^2 \quad (\varepsilon = 1\%) \quad \text{and} \quad L = 2.5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$$

$$\Rightarrow \text{lifetime} = 195 \text{ min (LER)} / 85 \text{ min (HER)}$$

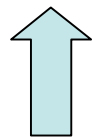
Lifetime due to beam-beam effects



- Lifetime will depend on betatron tunes.
- Dynamic emittance may relax lifetime.
- Momentum aperture may decrease due to beam-beam effect (dynamic beta).
- Still open question.

Summary of lifetime

	10^{35} PEP-II		10^{36} PEP-II		2.5×10^{35} KEKB	
	LER	HER	LER	HER	LER	HER
Quantum	6000	3000	6000	3000	long	long
Vacuum	180	360	120	240	600	600
Touschek	110	923	45	360	51	200 ?
Luminosity	150	75	50	25	195	85
Beam-beam	30	30	20	20	30 ?	30 ?
Total w/o b-b	47	57	20	21	38	54
Total	18	20	10	10	17 ?	19 ?



J.Seemen, Hawaii
 Super B-Factory WS,
 Jan, 2004.

Beam-beam parameters

- Luminosity is given by overlap integral:

$$L = \frac{f_c}{c} \int d^3x dt \rho_+(\vec{x}, t) \rho_-(\vec{x}, t) \times \sqrt{c^2(\vec{v}_+ - \vec{v}_-)^2 - (\vec{v}_+ \times \vec{v}_-)^2} \quad (\text{cm}^{-2}\text{s}^{-1})$$

$$\int d^3x \rho_{\pm}(\vec{x}, t) = N_{\pm} \quad f_c = c\beta/s_b$$

$$L = \frac{\gamma}{2er_e} \left(\frac{I \hat{\xi}_y}{\beta_y^*} \right) = 7.6 \times 10^{34} \cdot \frac{9.4(A) \cdot \hat{\xi}_y}{\beta_y^*(\text{cm})}$$

Beam-beam parameter is extracted from luminosity obtained from beam-beam simulations (Ohmi's definition).

$$\hat{\xi}_y = \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \left(\frac{R_L}{R_{\hat{\xi}_y}} \right) \cdot \xi_y$$

\uparrow \uparrow
 ~ 1 ~ 0.8

Luminosity strongly depends on betatron tunes.

$\hat{\xi}_y$ includes beam size ratio and ratio of reduction factors.