

# Measurements of Tune, Bunch Length and Bunch-by-Bunch Position



# Outline

- **Tune Measurement**

- Beam-Beam Tune Shift

- **Bunch Length Measurement**

- Monitor based on Beam Spectrum

- Bunch Lengthening and Shortening

- **Bunch-by-Bunch Position**

- BPM System

- Bunch-by-bunch Orbit

- **Summary**





# Beam-Beam Tune Shift

- Tunes in Beam-Beam Collision (H- & L- modes) :**

$$(\cos \mu_H + \cos \mu_L) - (\cos \mu_0^+ + \cos \mu_0^-) = -2\pi \{ \Xi_q^+ \sin \mu_0^+ + \Xi_q^- \sin \mu_0^- \}$$

- Coherent Beam-Beam Parameters:**

$$\Xi_q^\pm = \frac{N_\mp r_e}{\gamma_\pm} \frac{\beta_q^{0\pm}}{2\pi \Sigma_q (\Sigma_x + \Sigma_y)} R_q^\pm \quad \bar{\Xi}_q \approx \Xi_q^+ + \Xi_q^- \quad \Sigma_q = \sqrt{(\sigma_q^+)^2 + (\sigma_q^-)^2}$$

- Luminosity:**

$$L = \frac{f_0 N_b^+ \gamma^+}{r_e} \cdot \frac{T}{1+T} \cdot \left[ \frac{\Xi_y^+ + \Xi_y^-}{\beta_y^*} \right] \cdot \frac{R_L}{R_y^*} \quad T = \frac{I^- \gamma_-}{I^+ \gamma_+}$$

- Emittance:**

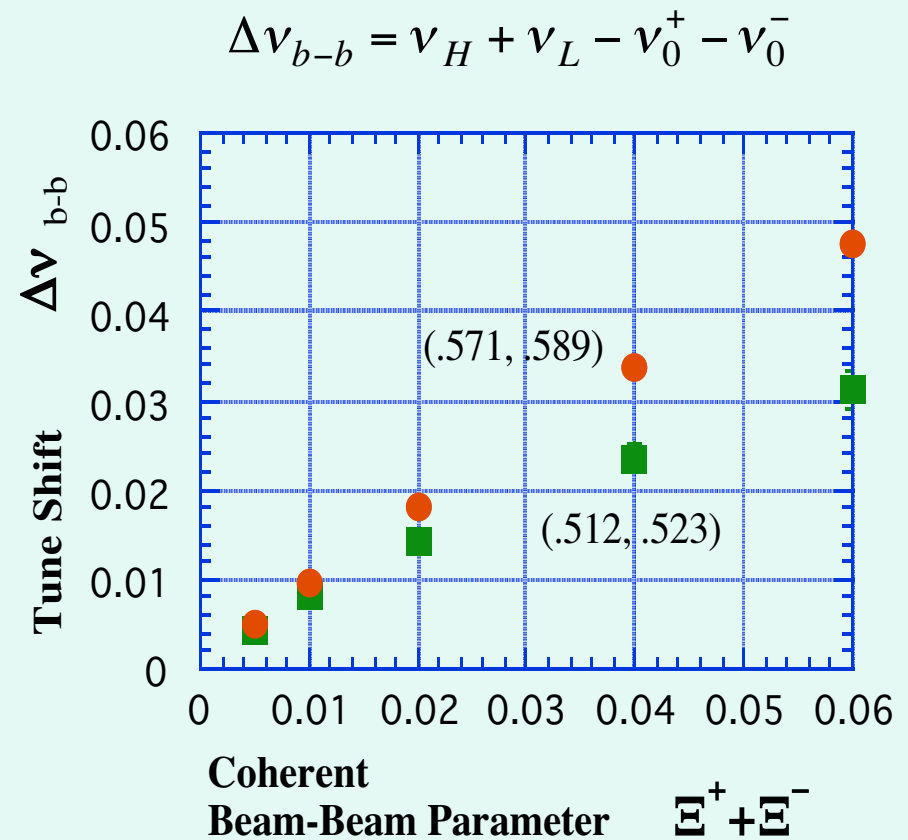
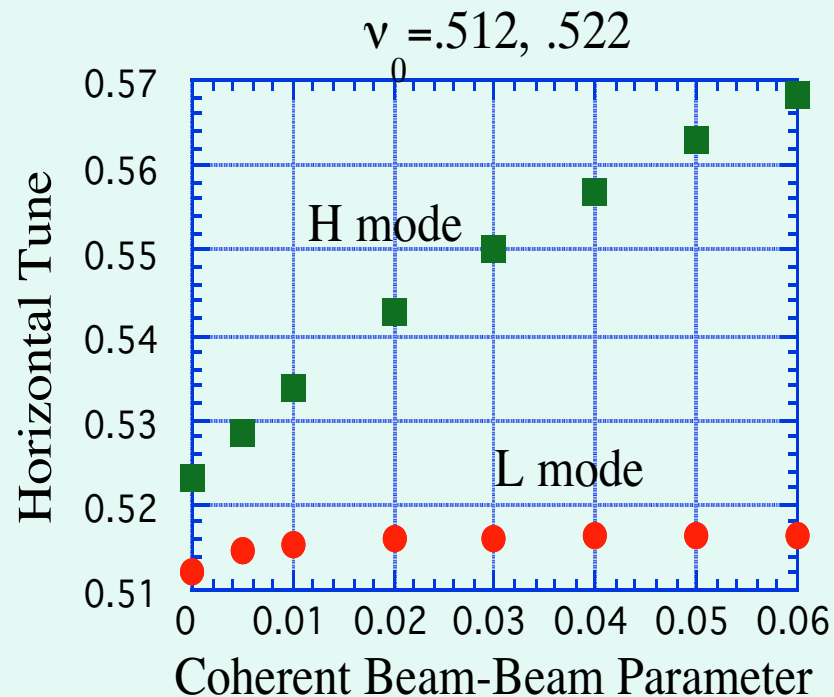
$R_q^*$  : reduction factors

$$\varepsilon_x^+ + \varepsilon_x^- = \frac{r_e}{\Xi_x^+ + \Xi_x^-} \cdot \frac{N^+}{2\pi \gamma^-} (1+T) \cdot R_x^* \quad \text{Assuming a flat beam and } \beta_x^+ \approx \beta_x^- = \beta_x^*$$



## Beam-Beam Tune Shift (cont'd)

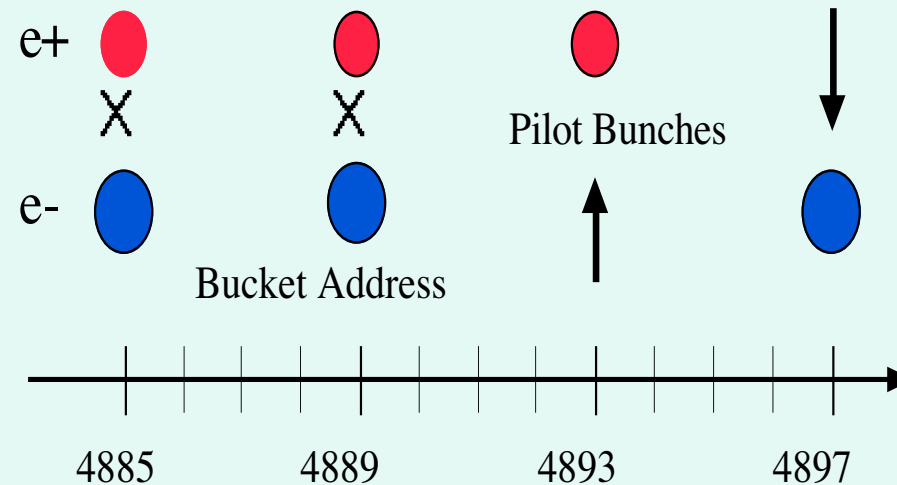
- Beam-Beam Tune Shift, calculation





## Measurement of Beam-Beam Tune

- Measurements of pilot bunch and collision bunches are useful for beam-beam study.
- Beam-beam tune shift is studied by measuring both tunes.



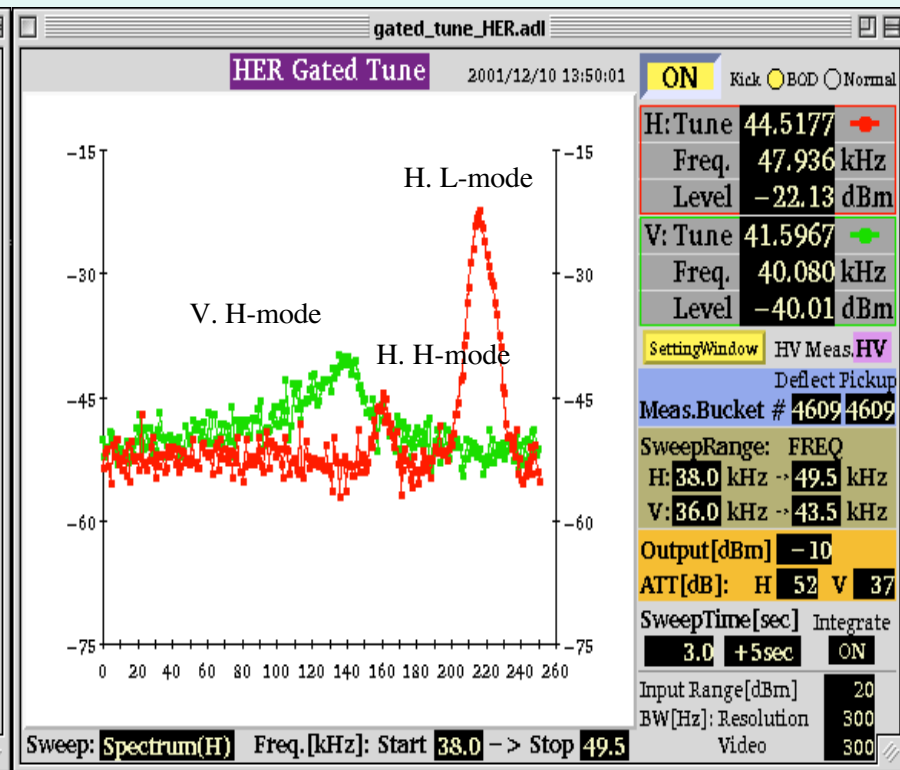
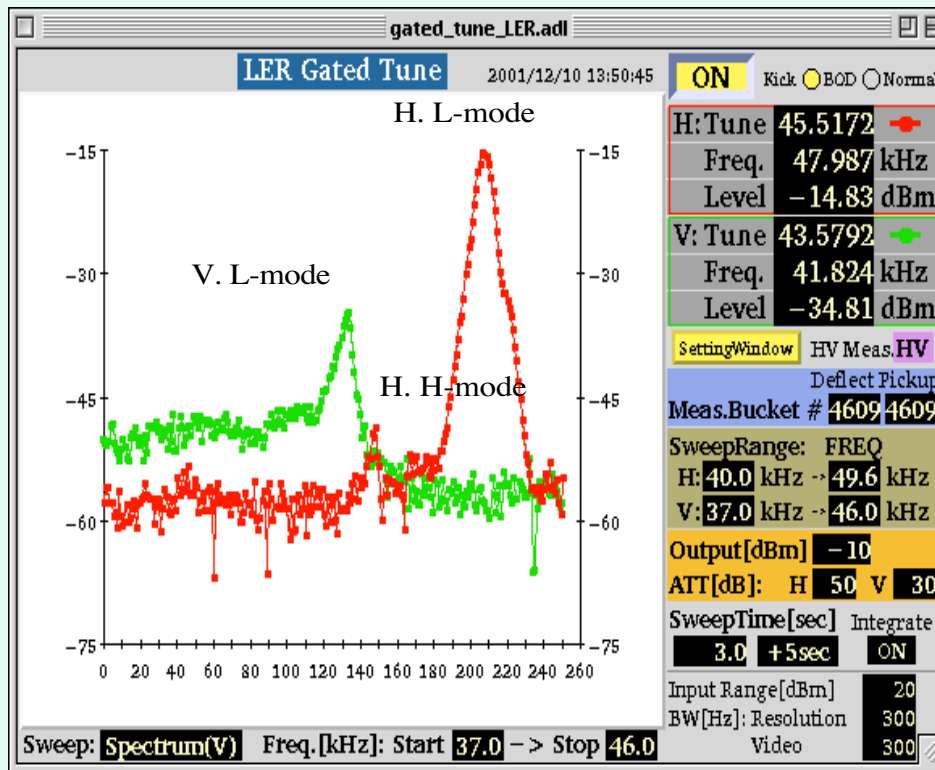


# Measurement of Beam-Beam Tune (cont'd)

## - Two beam-beam modes

LER

HER

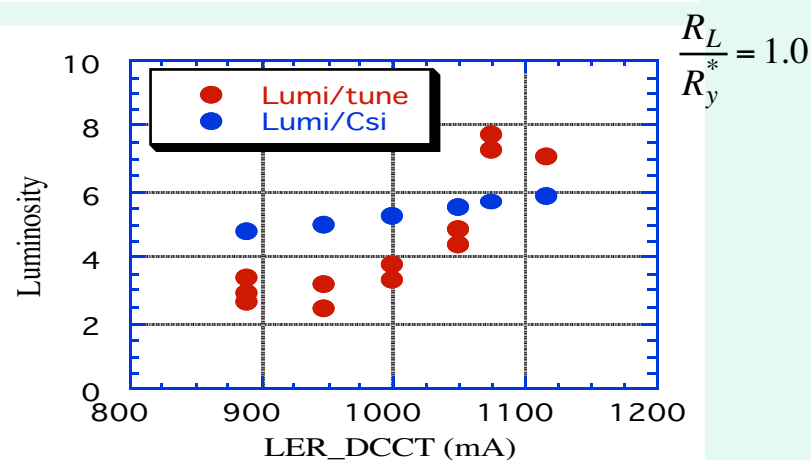
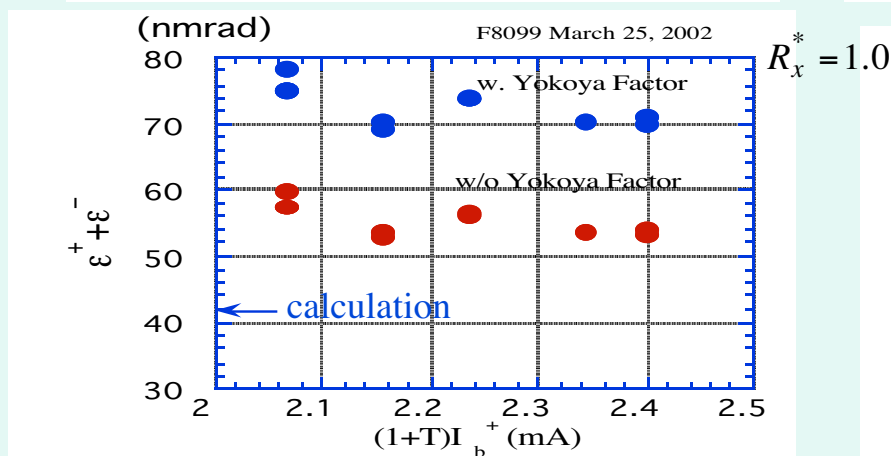
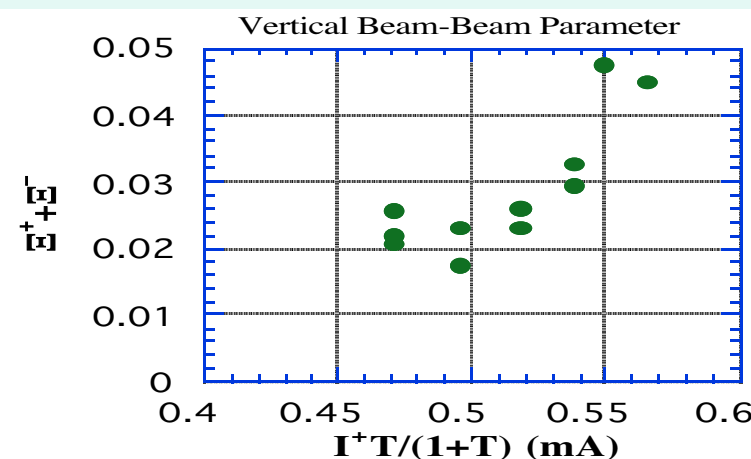
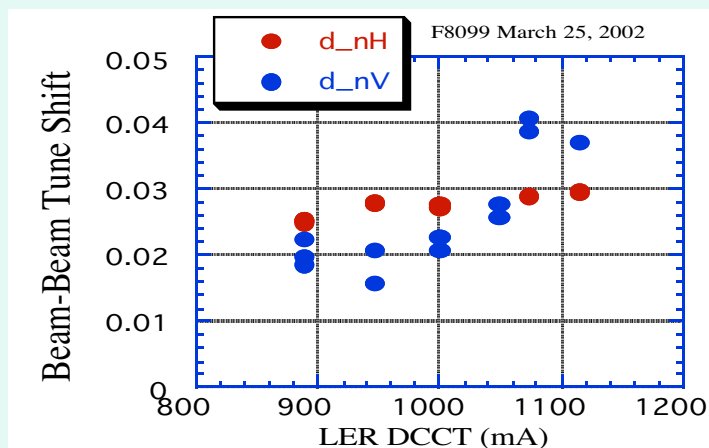


Non-Collision Tunes are .5124, .5712

.5221, .5903



# Measurement of Beam-Beam Tune (cont'd) - Current dependence

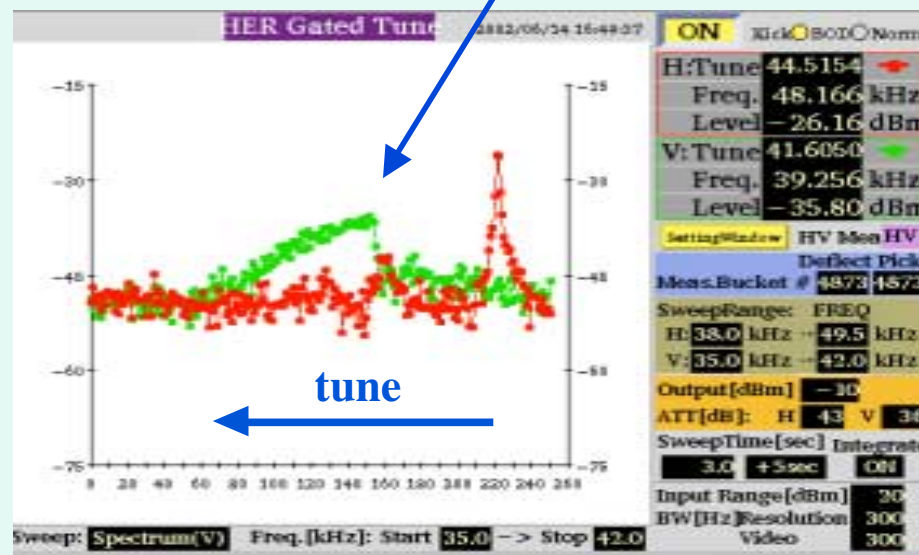
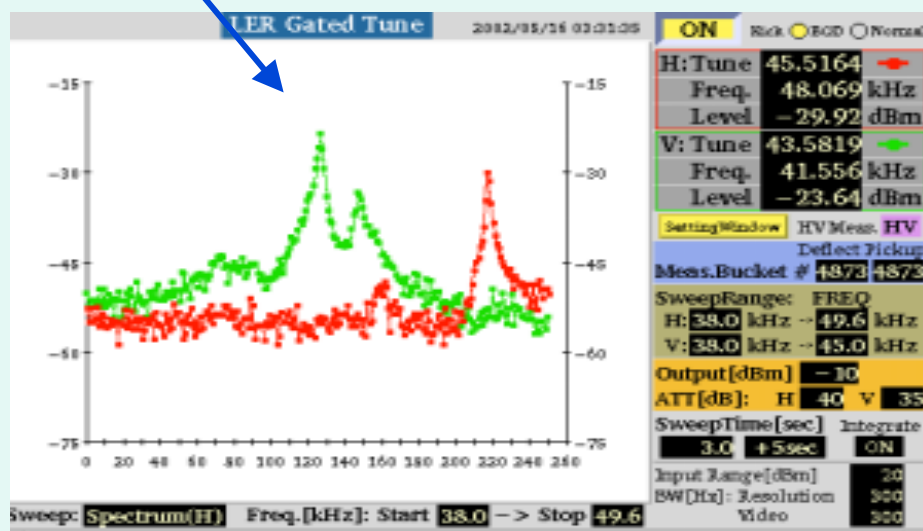




## Measurement of Beam-Beam Tune (cont'd) - Complexity

Two peaks appears, when vertical offset is given.

Nonlinearity in vertical spectrum



# Bunch Length Monitor based on Beam Spectrum

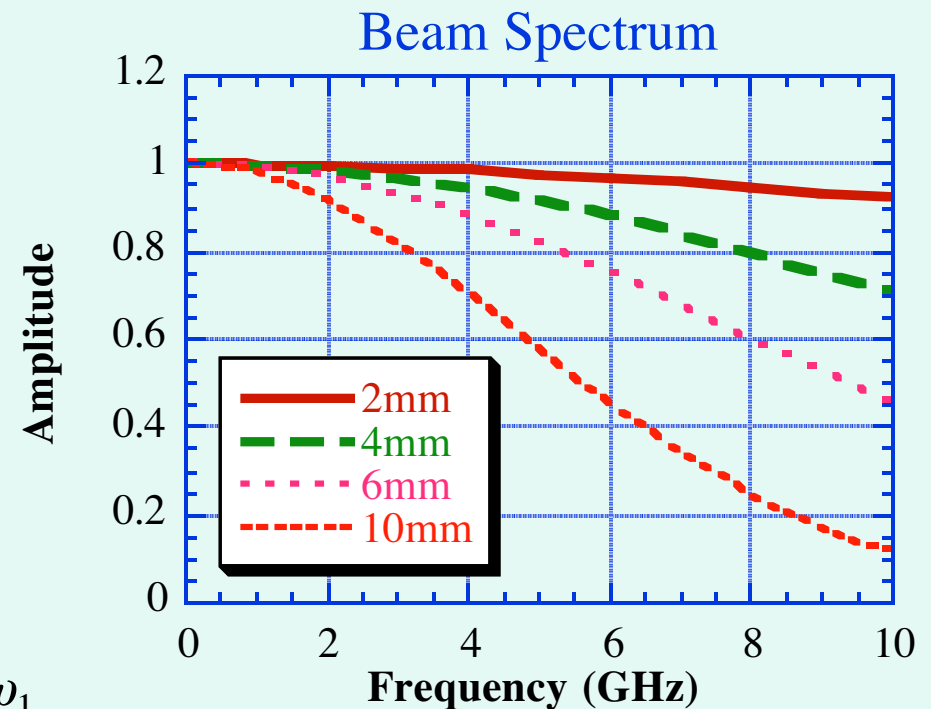
- Amplitude of Spectrum :

$$|F(\omega)| \approx I_0 \left\{ 1 - \frac{1}{2} \langle t^2 \rangle \omega^2 \right\} \quad \omega t < 1$$

- Rms Bunch Length :

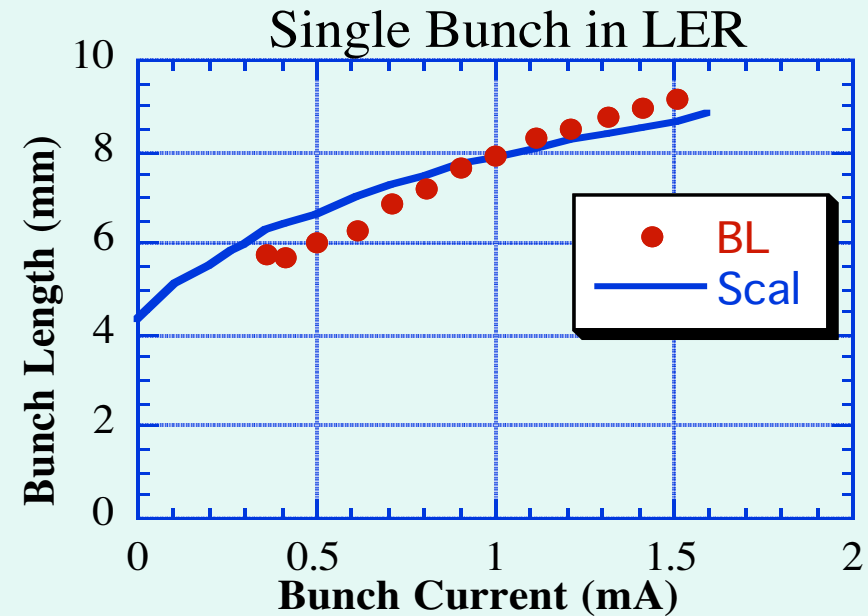
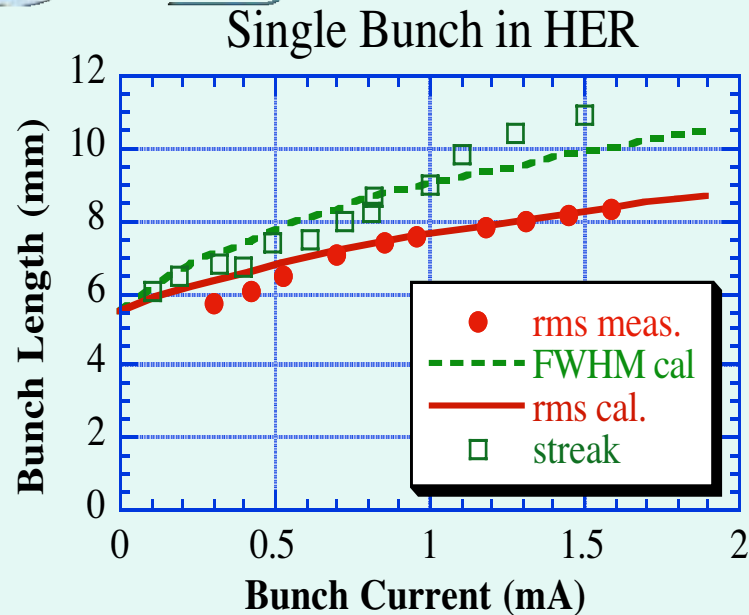
$$\sigma \equiv \sqrt{\langle t^2 \rangle} = \sqrt{\frac{2}{\Delta\omega^2} \ln \left| \frac{F(\omega_1)}{F(\omega_2)} \right|}$$

$$\Delta\omega = \omega_2 - \omega_1$$



**Note:** This measurement does *not* depend on bunch structures.

# Bunch Lengthening

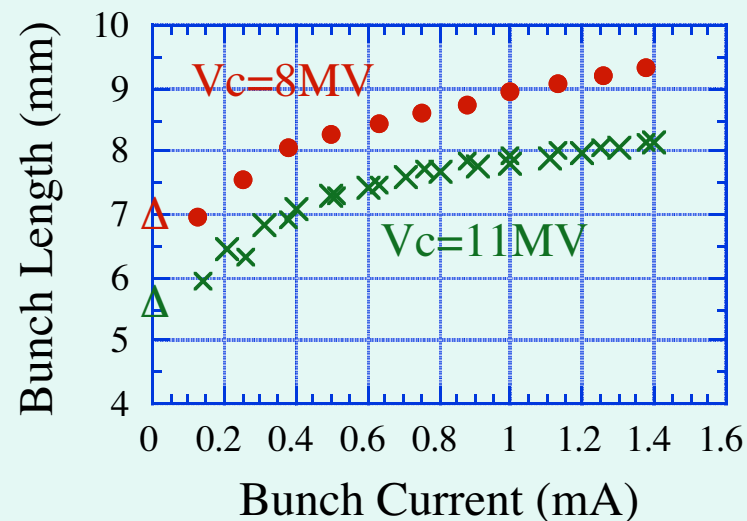
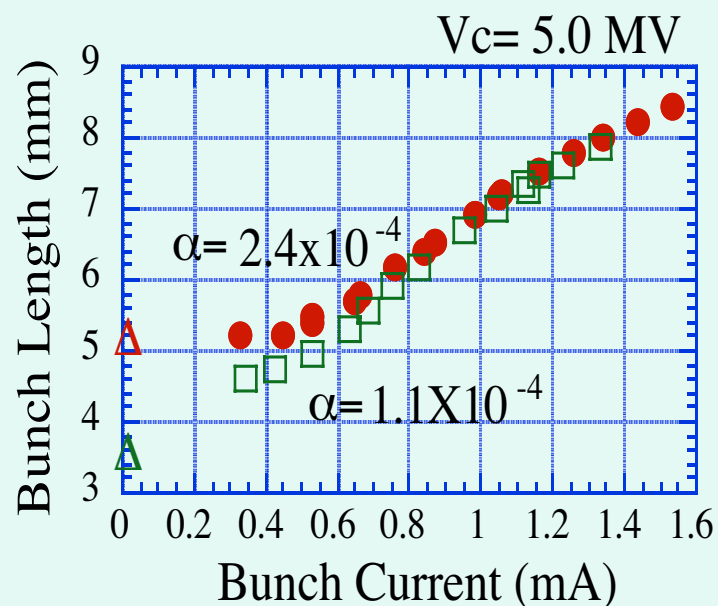


- Lines are calculated rms bunch length assuming purely inductive impedance, results in  $|Z_i / n| = 0.076 \Omega$  for HER and  $=0.072 \Omega$  for LER.
- Estimated impedance is **5 times** larger than the design of  $0.015 \Omega$ .
- Need to resolve the disparity between measurement and design.

## Reducing the bunch length

Natural bunch length :  $\sigma_0 = \frac{c \alpha \delta_\epsilon}{\omega_s}$

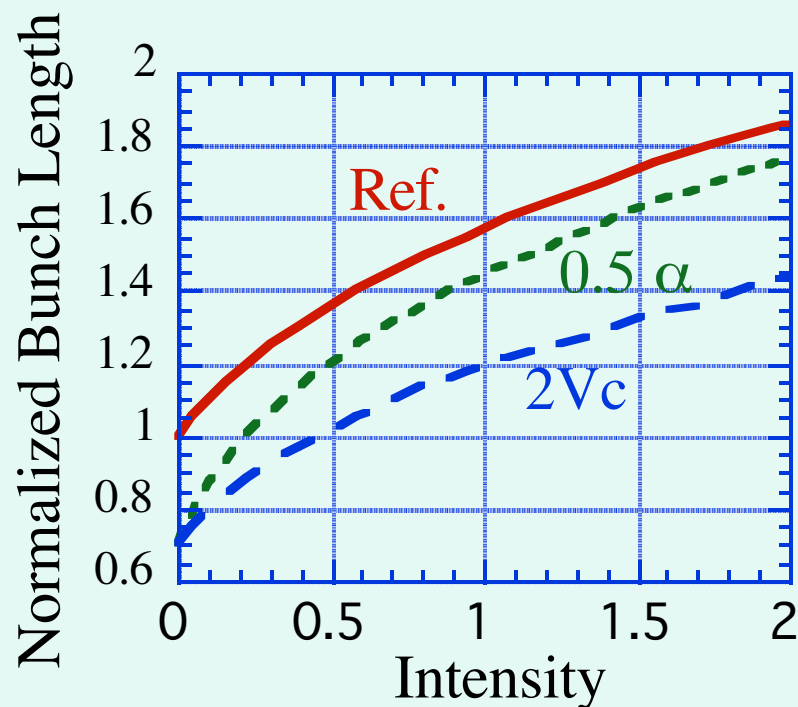
- (1) Reduce momentum compaction,  $\alpha$
- (2) Raise cavity voltage,  $V_c$





## Bunch Length Calculation with P.W.D.

- Both methods reduce B.L. to 70% at zero intensity.
- Higher  $V_c$  makes shorter B.L. at high intensity.



### Note:

- Higher  $V_c$  has advantage of beam loading.
- Short bunch length produces high HOM power.





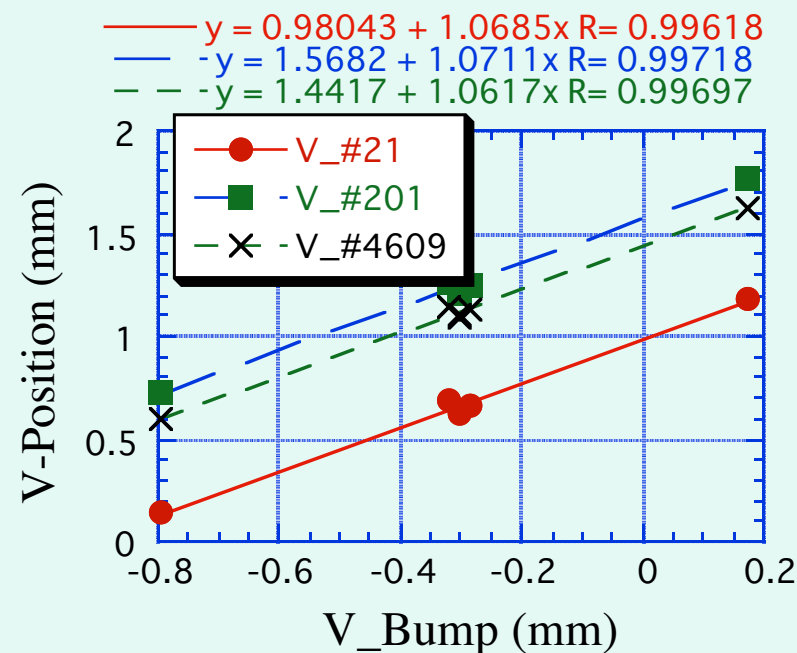
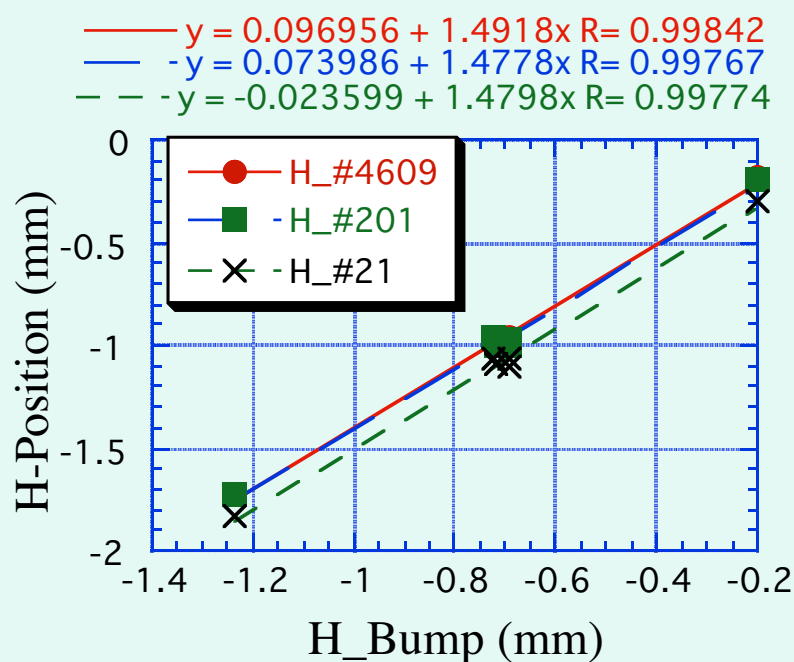
## Turn-by-Turn & Bunch-by-Bunch Beam Position Monitor

### *features*

- Share the button signal with the COD measurement.
- **Intensity, orbit and synchronous phase** are measured using an I/Q demodulator working at the rf frequency.
- The gate enables to measure the bunch-by-bunch parameters.
- Resolution :  $< 0.1$  degrees in phase,  $< 10 \mu\text{m}$  in orbit with averaging.

## Bunch-by-bunch Orbit - Effect of Orbit Bump

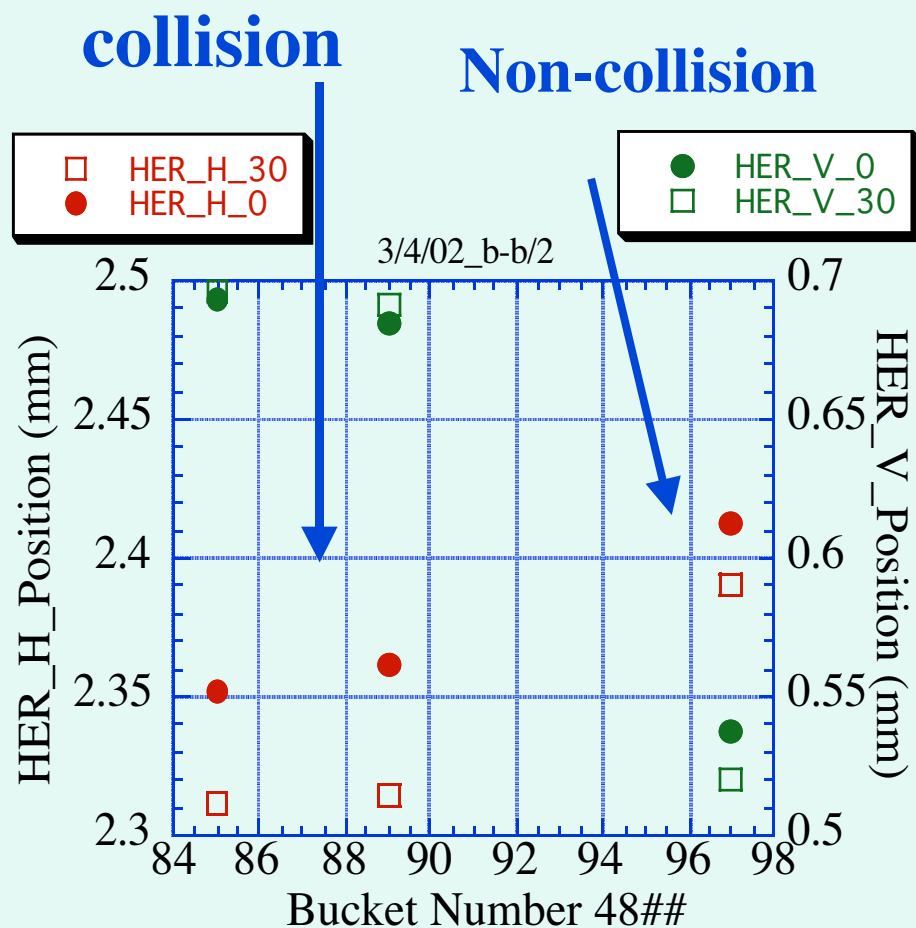
### ◆ Bunch-by-Bunch Position Sensitivity



Position Sensitivity for each bunch is consistent within 1%.

## Bunch-by-bunch Orbit

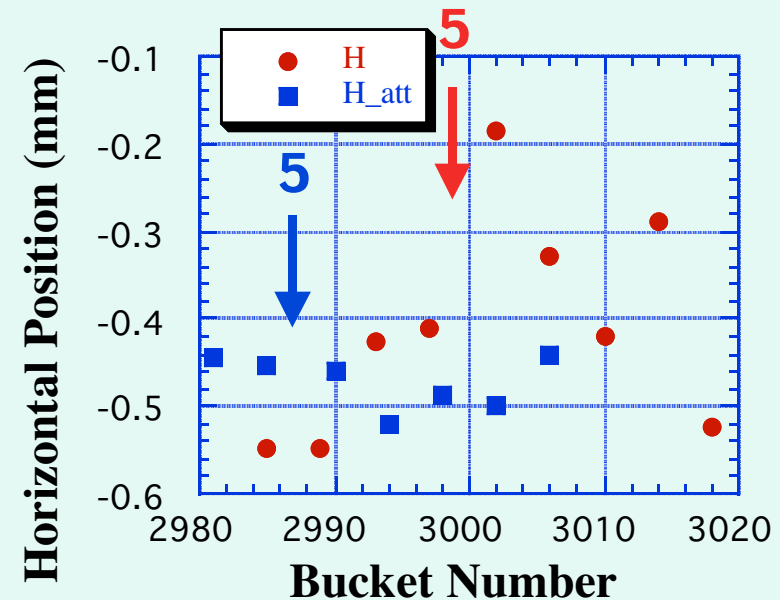
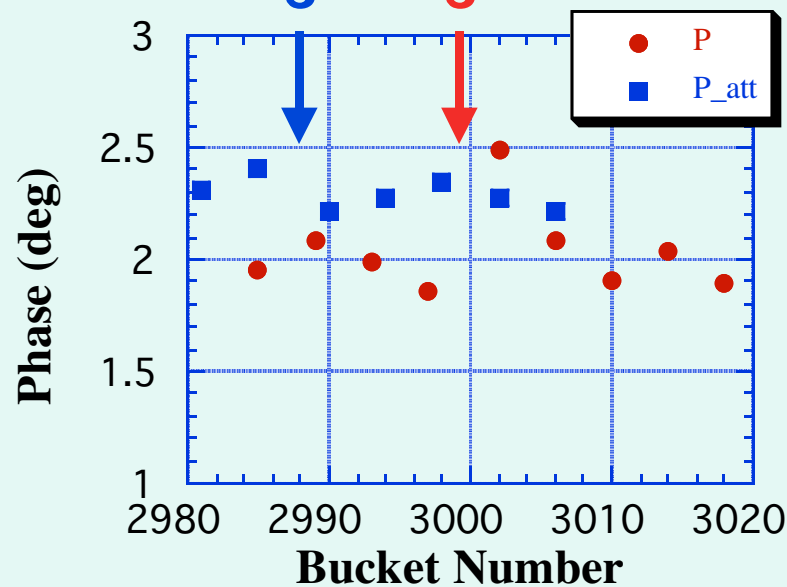
### - Effect of IP Horizontal Bump, *Preliminary*



- Orbit displacement exists between collision and non-collision bunches. **real ?**
- Collision offset makes an orbit displacement around the rings.
- Beam-beam effect can be estimated from an orbit difference between collision and non-collision bunches.

## Bunch-by-bunch Orbit in irregular 4-bucket spacing

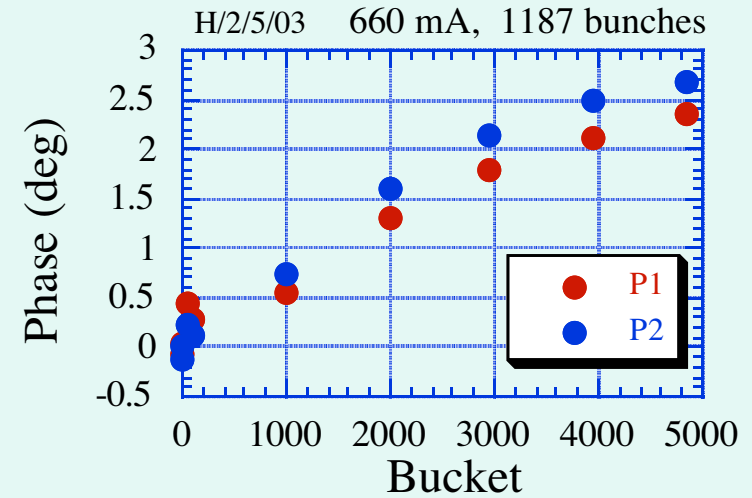
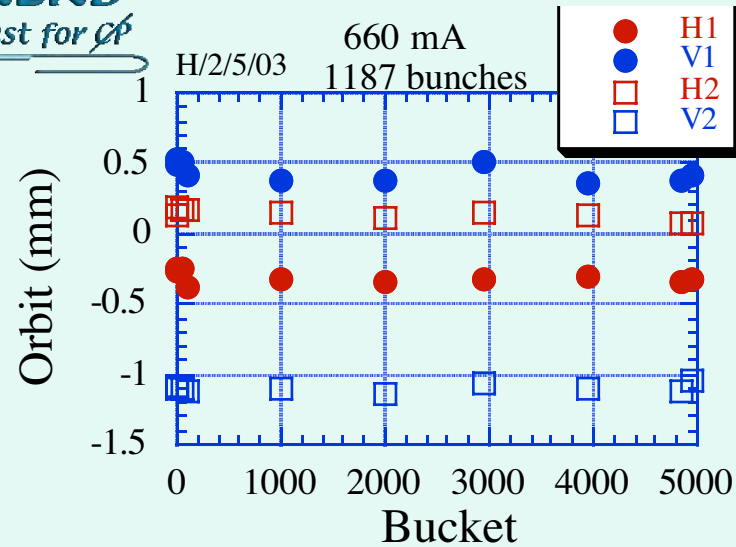
- We observed **jumps in phase and in orbits** at 5-bucket spacing.
- **Attenuators** inserted near the buttons **reduced the jumps**.
- Measurements are influenced by mismatch between buttons and the detector.



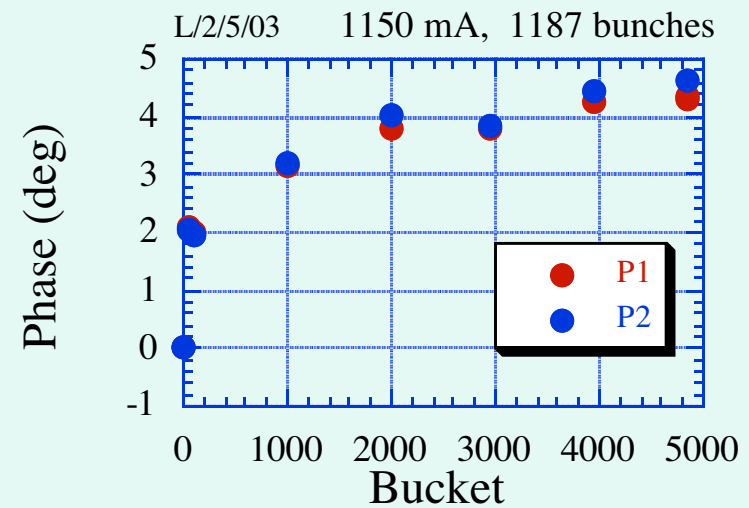
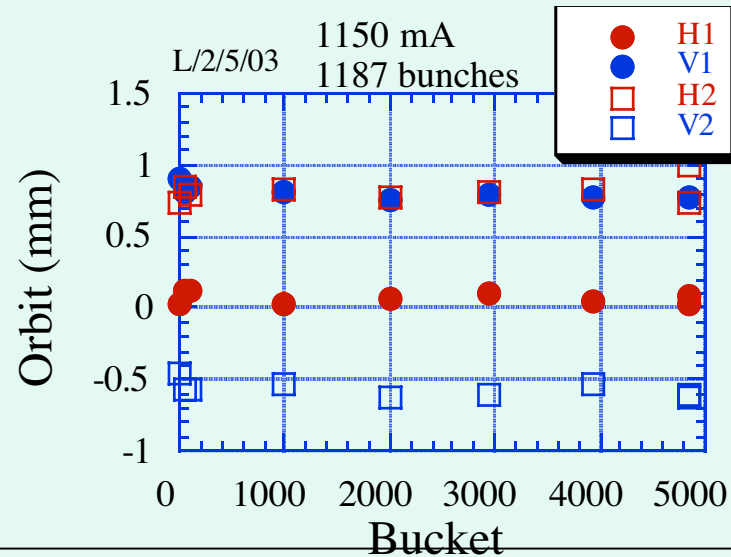


# Positions along Train

HER



LER





## Summary

- **Beam-beam tune shift**
  - Detected beam-beam modes under unequal tunes.
  - Estimated luminosity is roughly consistent with the luminosity monitor.
  - Estimated emittance is larger than calculation, suggests the dynamic effect.



## Summary (cont'd)

- **Bunch lengthening**
  - We need to check the impedance sources, to explain the unexpected bunch lengthening.
  - Raising  $V_c$  is more effective than reducing  $\alpha$ , to make the bunch length short .
- **Bunch-by-bunch position**
  - Beam-beam offset could be measured from an orbit displacement.
  - Orbit along train stays within +/- 0.1 mm.